

Example of Computing a Minimal Cover

Let $R = R(A, B, C, D, E, G, H)$

$F = \{1. CD \rightarrow AB,$
2. $C \rightarrow D,$
3. $D \rightarrow EH,$
4. $AE \rightarrow C,$
5. $A \rightarrow C,$
6. $B \rightarrow D\}.$

The process of computing a minimal cover of F is as follows:

- (1) Break down the right hand side of each fd's.

After performing step (1) in the algorithm, we get

$F' = \{$
1. $CD \rightarrow A,$
2. $CD \rightarrow B,$
3. $C \rightarrow D,$
4. $D \rightarrow E,$
5. $D \rightarrow H,$
6. $AE \rightarrow C,$
7. $A \rightarrow C,$
8. $B \rightarrow D$
 $\}.$

- (2) Eliminate redundancy in the left hand side by eliminating redundant attributes:

The fd 1. $CD \rightarrow A$ is replaced by $C \rightarrow A$.

This is because $C \rightarrow D$ a $(F') +$, hence $C \rightarrow CD$ a $(F') +$;

from $C \rightarrow CD$ a $(F') +$ and $CD \rightarrow A$ a F' , by transitivity, we have $C \rightarrow A$ a $(F') +$
and hence $CD \rightarrow A$ should be replaced by $C \rightarrow A$.

Similarly for fd 2. : $CD \rightarrow B$ is replaced by $C \rightarrow B$,

Similarly for fd 6. : $AE \rightarrow C$ is replaced by $A \rightarrow C$.

$F' = \{1. C \rightarrow A, 2. C \rightarrow B, 3. C \rightarrow D, 4. D \rightarrow E, 5. D \rightarrow H, 6. A \rightarrow C, 7. B \rightarrow D\}$
after step (2).

- (3) Remove redundant fd's. The fd $C \rightarrow D$ is eliminated because it can be derived from $C \rightarrow B$ and $B \rightarrow D$ and hence it is redundant.

The F' now becomes **$\{1. C \rightarrow A, 2. C \rightarrow B, 3. D \rightarrow E, 4. D \rightarrow H, 5. A \rightarrow C, 6. B \rightarrow D\}$** , which is the only minimal cover of F .